



Convection velocity in HID lamp including acoustic resonance

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I. Motivation

Understand the interaction between acoustics resonances and the plasma instabilities.



2D axi-symmetric model used finites elements has been implemented in Comsol for a HID lamp operated at high frequency including the influence of acoustic velocity .

II. Model

a. Temperature

For to compute the temperature in the burner, we need three equations

1. Convection and Conduction equation:

$$\nabla \cdot (-k \nabla T) = Q - \rho C_p \vec{U} \cdot \nabla T$$

2. Incompressible Navier-Stokes equation (convection velocity):

$$\rho (\vec{U} \cdot \nabla) \vec{U} = \nabla [-p \vec{I} + \eta (\nabla U + (\nabla U)^T)] + \vec{F}$$

3. Poisson's equation (electrical field):

$$\nabla \cdot (-\sigma \nabla V) = 0$$

b. Acoustic Pressure

The modeling of acoustic resonances in the burner is performed by using the eigenfrequency analysis :

$$\nabla \cdot \left(-\frac{1}{\rho} \nabla p \right) - \frac{\lambda_j p}{c_j^2 \rho} = 0$$

c. Acoustic Amplitude

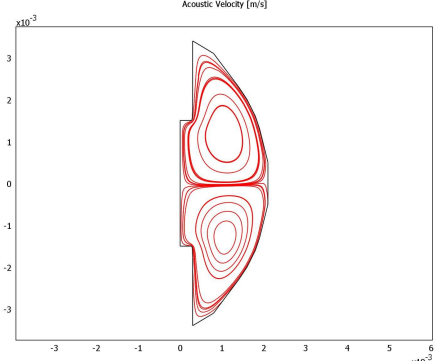
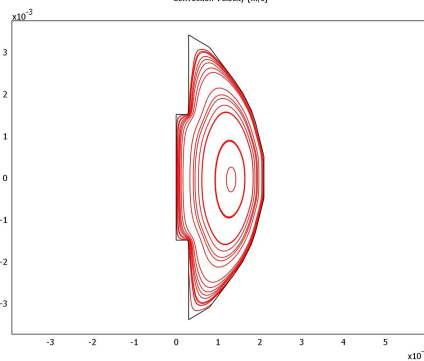
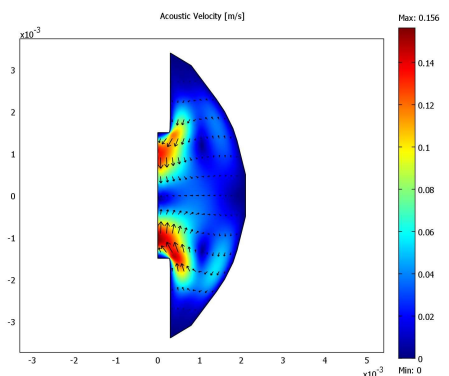
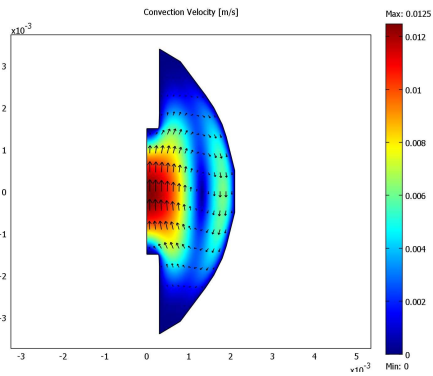
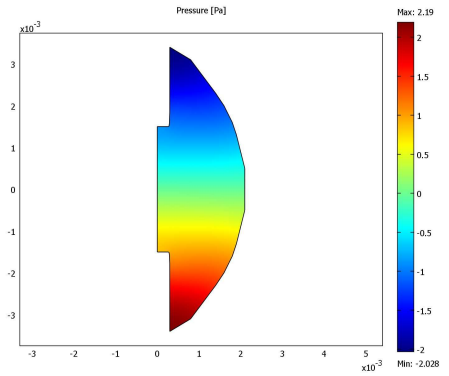
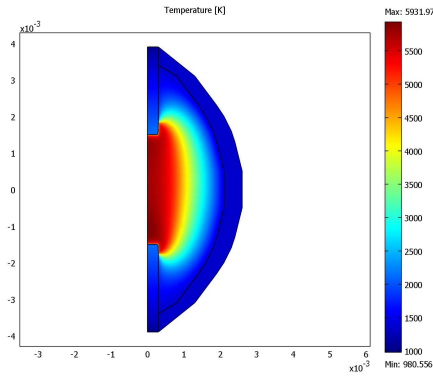
For to take into account losses to the walls and in the volume, we compute the amplitude of AR

$$A_j(\omega) = i \frac{A_j \omega}{\omega^2 - \omega_j^2 + i \frac{\omega \omega_j}{Q_j}}$$

d. Streaming Acoustic

As a non-linear second order effect of the acoustic wave that has a time-averaged amplitude different to zero, a vortex acoustic flow develops in the burner and his force, for the direction of axis j, is written:

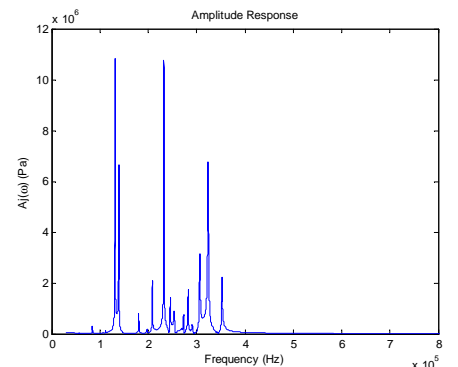
$$F_j = - \frac{\partial \overline{\rho v_j v_j}}{\partial x_j}$$



*For all figures, Pressure=40.10⁵ [Pa] and Current=0.25 [A]

III. Conclusion

The appearance of fluxes combining convection and acoustic streaming may be responsible for instabilities in HID lamp and it give us a beginning of explanation for the relation between the acoustic resonances and the arc instabilities.



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